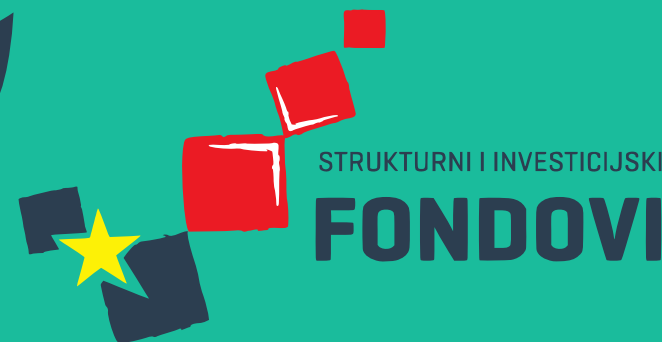


The 8th Community Community Coordinated Modeling Center Workshop



THE DRAG-BASED MODEL

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General classification of space-weather models

- The DBM: a „tool“ for prediction of ICMEs propagation in the heliosphere → primary task for space-weather forecasting
- modeling and forecasting can be divided:
 - a) purely empirical/statistical methods
 - b) kinematical-empirical methods
 - b/c) analytical (M)HD-based models (DBM)
 - c) numerical MHD-based models

The DBM hypothesis

- The DBM hypothesis at large heliocentric distances:
 - the Lorentz force ceases in upper corona
 - ICME dynamics is solely governed by interaction with solar wind (ambient) ← observational facts:
 - fast CME → decelerate
 - slow CME → accelerate
- } $v \rightarrow w$
- collisionless environment:
 - low viscosity
 - low resistivity → dissipative processes are negligible
 - momentum and energy are transferred by magnetosonic waves

The DBM equations in general form

- At heliocentric distances beyond $R \geq 15 r_s$:
- net acceleration (drag is dominant): $a = a_L + a_g + a_d$
- equation of motion in quadratic form (Cargill, 2004):

$$R''(t) = -\gamma(R) [R'(t) - w(R)] |R'(t) - w(R)|$$

- parameter γ :

$$\gamma \propto C_d \frac{A \rho_{SW}}{M} \quad \bullet \text{ for } R \gg 1r_s \Rightarrow M = M_i + M_v = \text{const.}$$

- LDB density expression (Leblanc et al., 1998):

$$n_0(R) = \frac{k_2}{R^2} + \frac{k_4}{R^4} + \frac{k_6}{R^6} \text{ for } R > 1.8$$

$$k_2 = 3.3 \times 10^5 \text{ cm}^{-3}, k_4 = 4.1 \times 10^6 \text{ cm}^{-3}, k_6 = 8.0 \times 10^7 \text{ cm}^{-3}$$

Solar wind perturbation

- stationary and isotropic
- density flux conservation
- unperturbed solar-wind speed becomes:

INPUT:
 $w(R), w_\infty, \gamma_\infty$

$$w_0(R) = w_\infty \left(1 + \frac{k_4/k_2}{R^2} + \frac{k_6/k_2}{R^4} \right)^{-1} \quad \left[w_\infty = \lim_{R \rightarrow \infty} w_0(R) \right]$$

- total solar-wind speed with perturbation term $w_p(R)$:

$$w(R) = \begin{cases} w_0(R) + w_p(R), & R_1 < R < R_2 \\ w_0(R), & \text{otherwise} \end{cases}$$

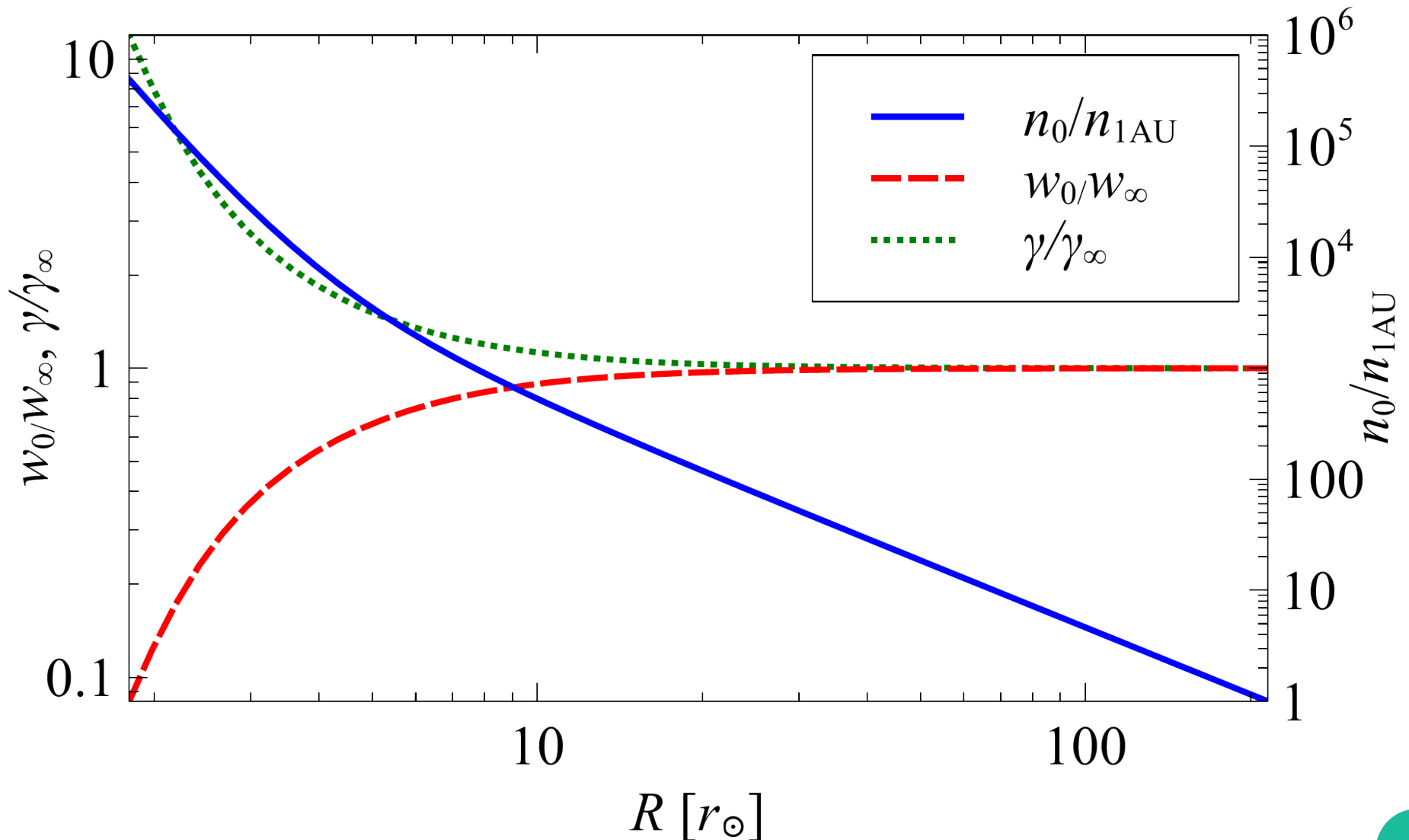
+ „Cone geometry“:
 $A \propto R^2$

- leads to:

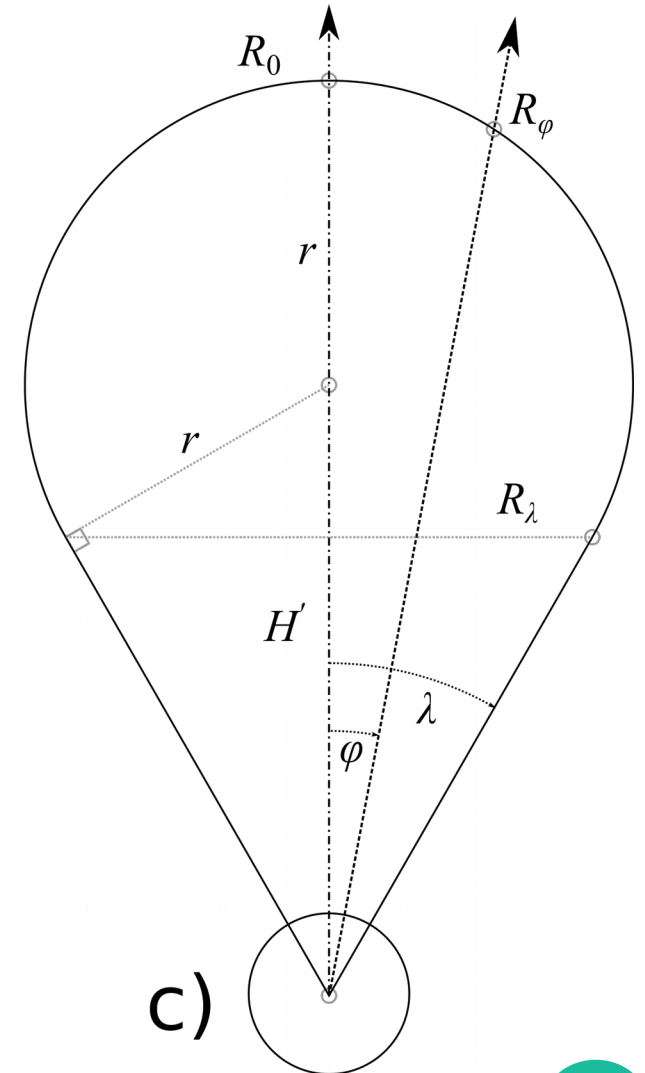
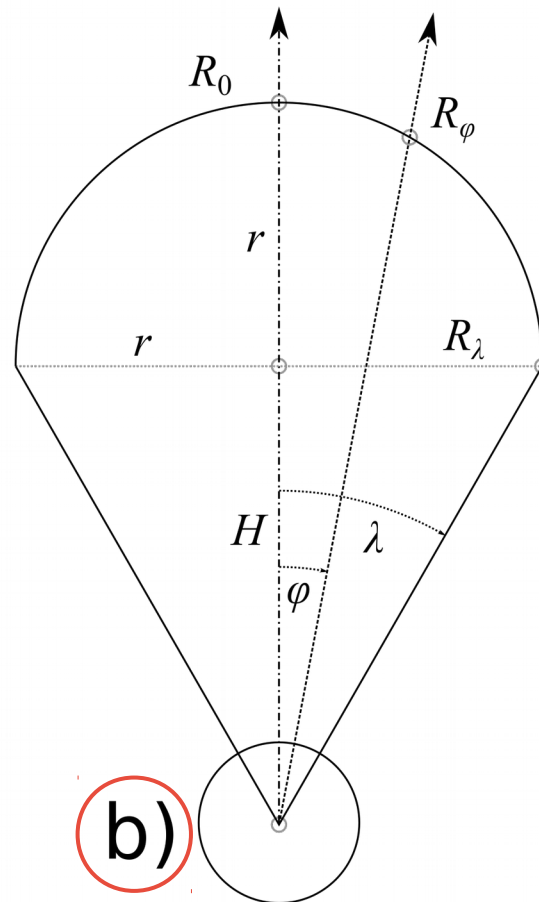
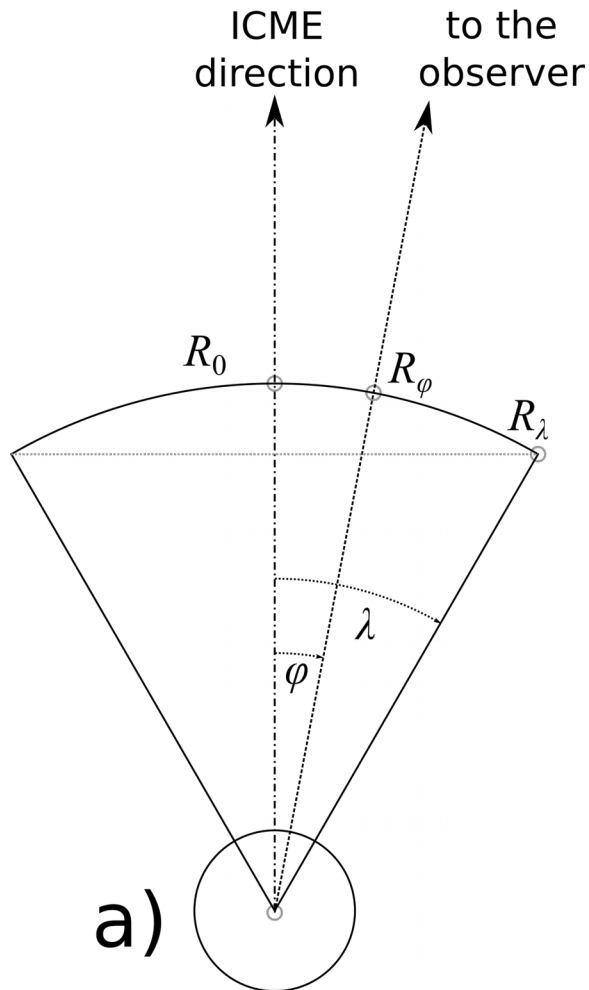
$$\gamma(R) = \gamma_\infty \frac{w_\infty}{w(R)}; \quad n(R) = \frac{k_2}{R^2} \frac{w_\infty}{w(R)} \quad \left[\gamma_\infty = \Gamma \times 10^{-7} \text{ km}^{-1} \right]$$

$\left[\gamma_\infty = \lim_{R \rightarrow \infty} \gamma(R) \right]$

Parameter γ , SW density and speed

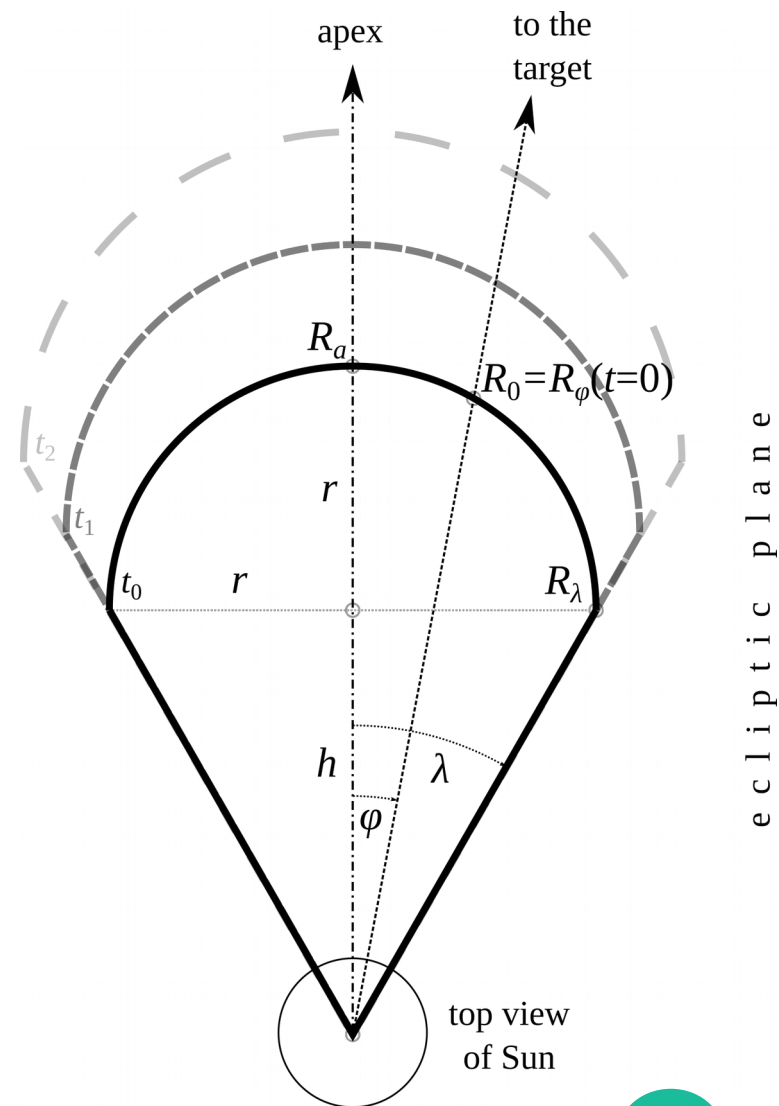


Options of ICME cone-geometry



DBM with constant w and self-similar CME geometry

- solar-wind speed w :
 - isotropic and constant
 - parameter γ is constant as well
- „self-similar“ CME expansion:
 - the initial cone-shape of CME is preserved during its interplanetary propagation
- for a given set of input parameters the model provides the ICME Sun-“target” transit time, the arrival time, and the impact speed



Basic $w=const.$ & SS-expansion (<http://oh.geof.unizg.hr/~tomislav/CDBM-SS/>)

Forecasting the Arrival of ICMEs: The Drag-Based Model with constant solar wind speed and self-similar CME expansion

Basic DBM | Advanced DBM | Documentation

CME take-off **date**: Apr 8 2016

CME take-off **time (UTC)**: 15 h 10 min

γ - constant drag parameter: 0.2 $\times 10^{-7} \text{ km}^{-1}$

w - constant solar wind speed: 450 km/s

R_0 - starting radial distance of CME: 20 r_{Sun}

v_0 - speed of CME at R_0 : 1000 km/s

Select **target** from the list: Earth Select

Calculate Reset!

© Tomislav Žic, Hvar Observatory, 2013

Zadnja obnova stranice: 8.4.2016.

Advanced $w=const.$ & SS-expansion (<http://oh.geof.unizg.hr/~tomislav/CDBM-SS/>)


Forecasting the Arrival of ICMEs: The Drag-Based Model with constant solar wind speed and self-similar CME expansion

Basic DBM

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Documentation

CME take-off **date**:

Apr ▼ 8 ▼ 2016 

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15 ▼ h 10 ▼ min

γ - constant drag parameter:

0.2 $\times 10^{-7} \text{ km}^{-1}$

w - constant solar wind speed:

450 km/s

R_0 - starting radial distance of CME:

20 r_{Sun}

v_0 - speed of CME at R_0 :

1000 km/s

λ - CME's angular half-width:

30 deg

φ_{CME} - central meridian distance of source region:

0 deg

Select **target** from the list:

Earth ▼

© Tomislav Žic, Hvar Observatory, 2013

Zadnja obnova stranice: 8.4.2016.

Results $w=const.$ & SS-expansion (<http://oh.geof.unizg.hr/~tomislav/CDBM-SS/>)

Forecasting the Arrival of ICMEs: The Drag-Based Model with constant solar wind speed and self-similar CME expansion

Results | Kinematic plot | CME geometry plot | Documentation

Output:

CME arrival at target (date & time): 14.04.2016 at 18h:12min

Transit time: 50.20 h

Impact speed at target (at 1 AU): 634 km/s

Input parameters:

CME take-off date & time: 12.04.2016 at 16h:00min

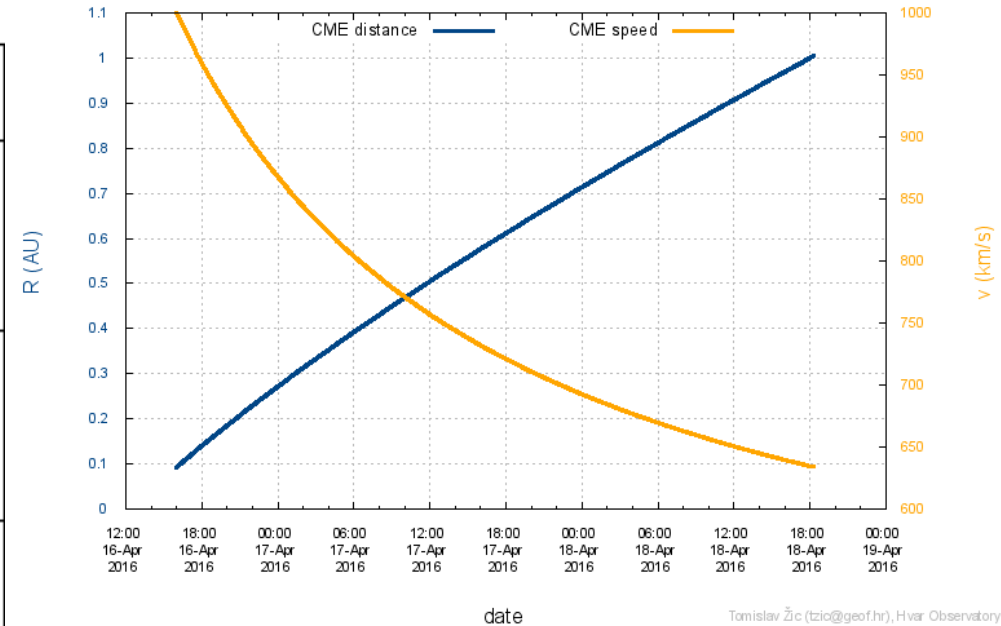
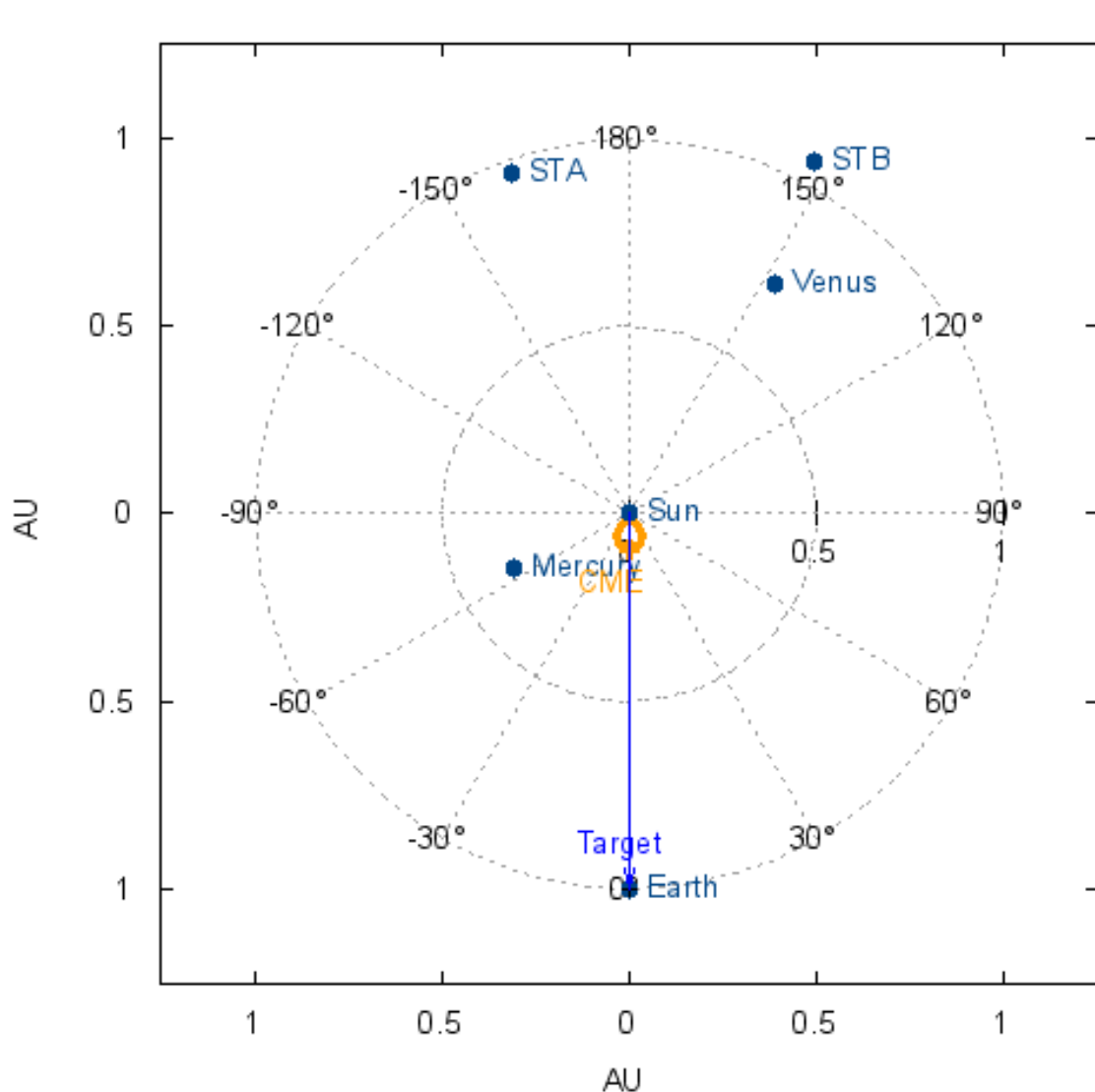
$\gamma = 0.2 \times 10^{-7} \text{ km}^{-1}$, $w = 450 \text{ km/s}$,

$R_0 = 20 r_{\text{Sun}}$, $v_0 = 1000 \text{ km/s}$, $\lambda = 30^\circ$, $\varphi_{\text{CME}} = 0^\circ$

$R_{\text{target}} = 1 \text{ AU}$, $\varphi_{\text{target}} = 0^\circ$

Calculated in 3.15 seconds.

Plots $w=const.$ & SS-expansion (<http://oh.geof.unizg.hr/~tomislav/CDBM-SS/>)



- ↑ UP: Propagation of '+ CME' point in geometry plot
- ← LEFT: Ecliptic plane cross-section of CME propagation

Online applications of DBM with $w=const.$ & SS-expansion

Used on web pages of:

• Hvar Observatory - Forecasting the Arrival of ICMEs:
<http://oh.geof.unizg.hr/DBM/dbm.php>

• The COMESEP alert system:
<http://www.comesep.eu/alert/>

• ESA Expert Service Center for Solar & Heliospheric Weather:
<http://swe.uni-graz.at/index.php/services/cme-forecast>

• Space Weather Database Of Notifications, Knowledge, Information (DONKI):
<http://kauai.cmc.gsfc.nasa.gov/DONKI/>

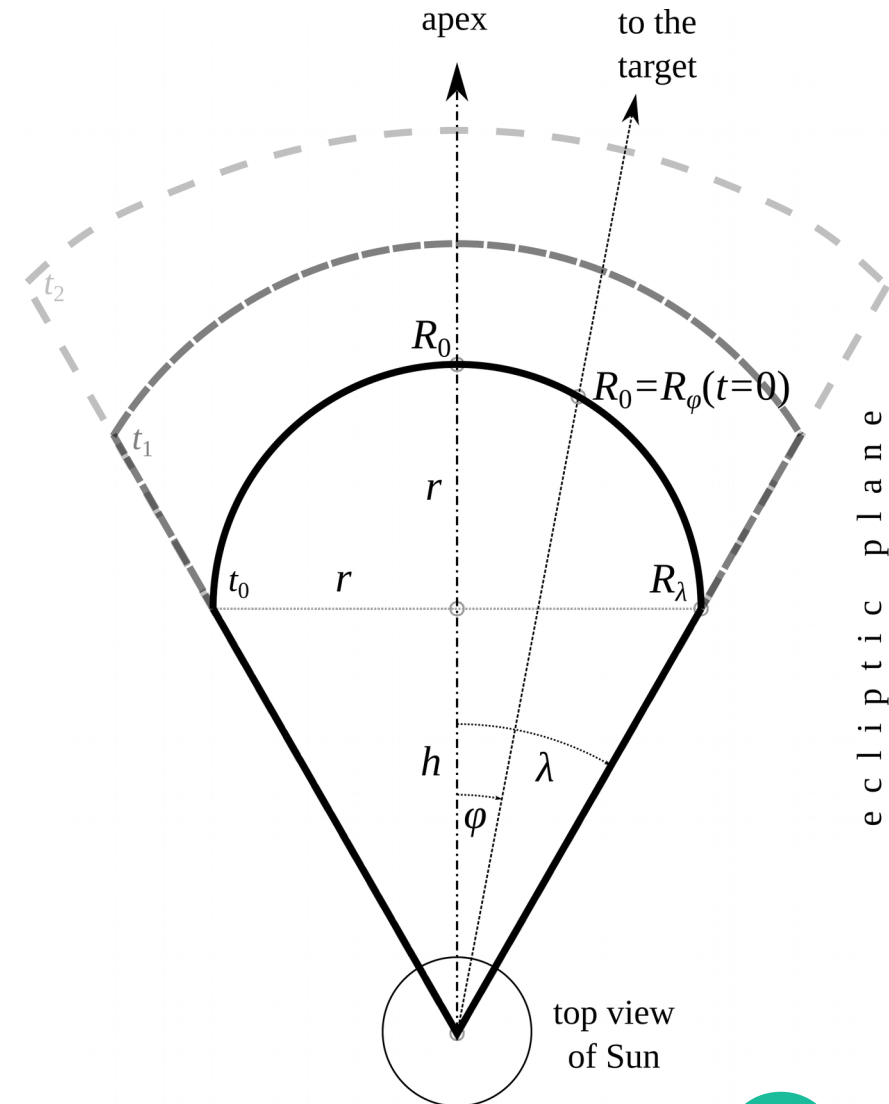
• CME Arrival Time Scoreboard - NASA Space Weather Research Center:
<http://swrc.gsfc.nasa.gov/main/cmemodels>

(courtesy of Leila M. Mays)

CCMC Contact:
 Leila Mays
 (M.Leila.Mays@nasa.gov)

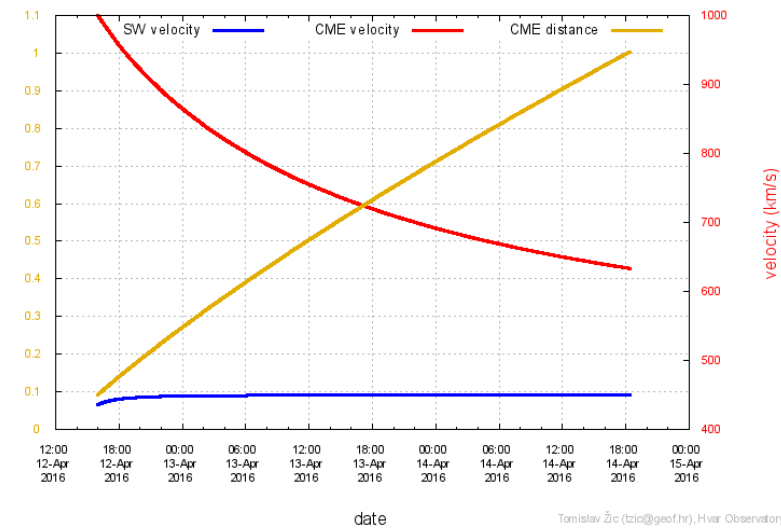
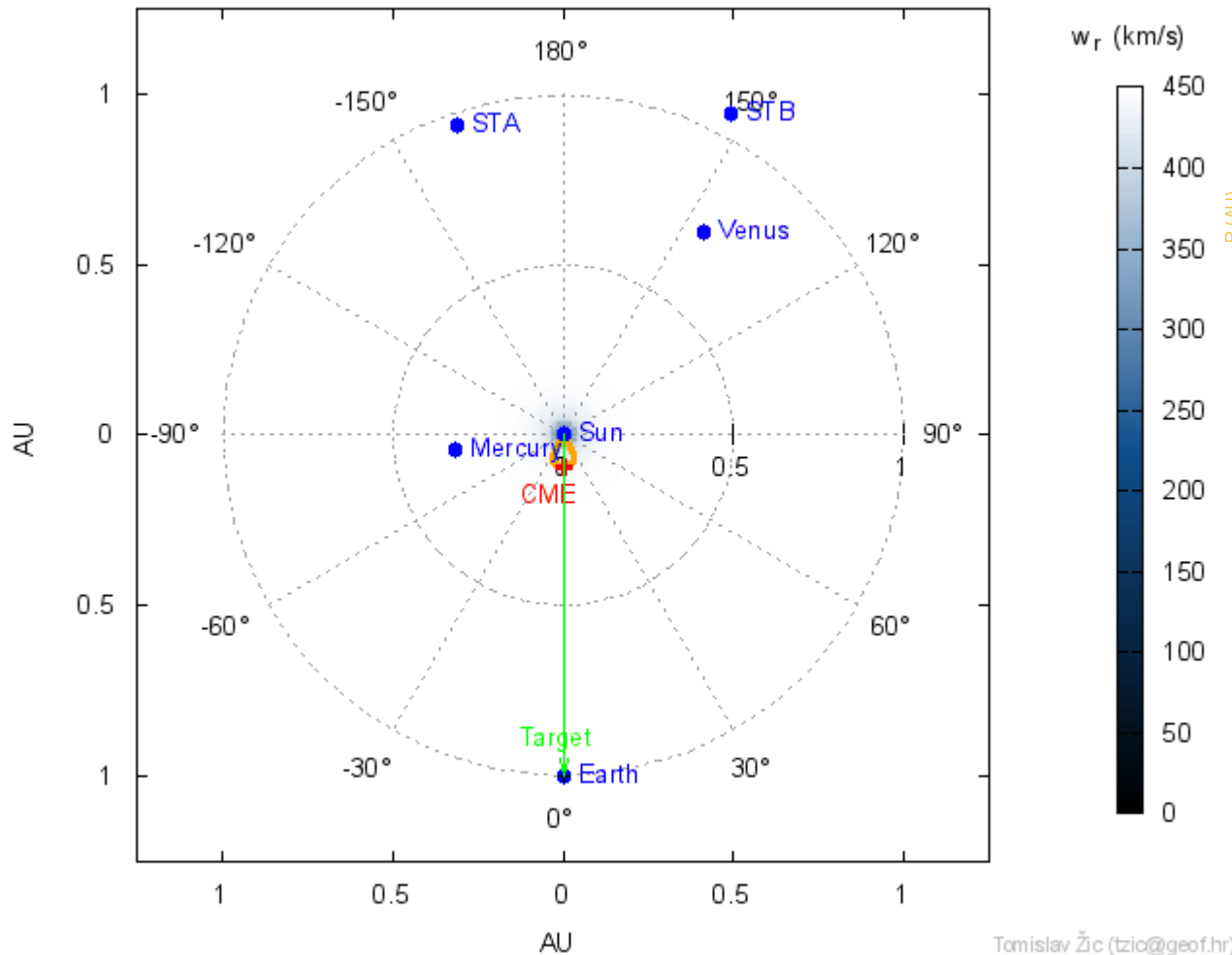
DBM with $w(R)$ and CME leading-edge flattening

- solar-wind speed w :
 - is radially dependent: $w(R)$
 - parameter γ becomes function of radial distance as well: $\gamma(R)$
- each CME leading-edge segment propagates independently
 - the initial cone-geometry flattens



Plots $w(R)$ & CME edge flattening

(<http://oh.geof.unizg.hr/~tomislav/DBM/>)



Output:

- CME arrival at target (date & time): 14.04.2016 at 18h:20min
- Transit time: 50.35 h
- Impact speed at target (at 1 AU): 633 km/s

Input parameters:

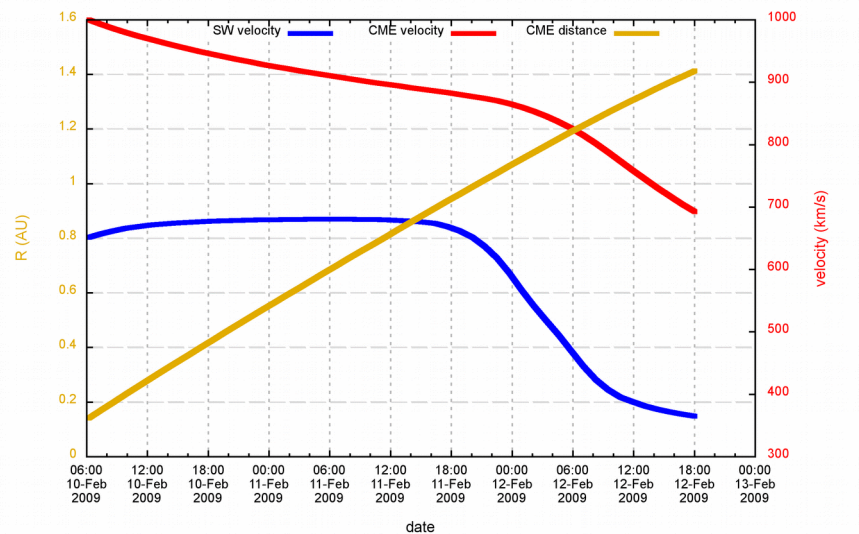
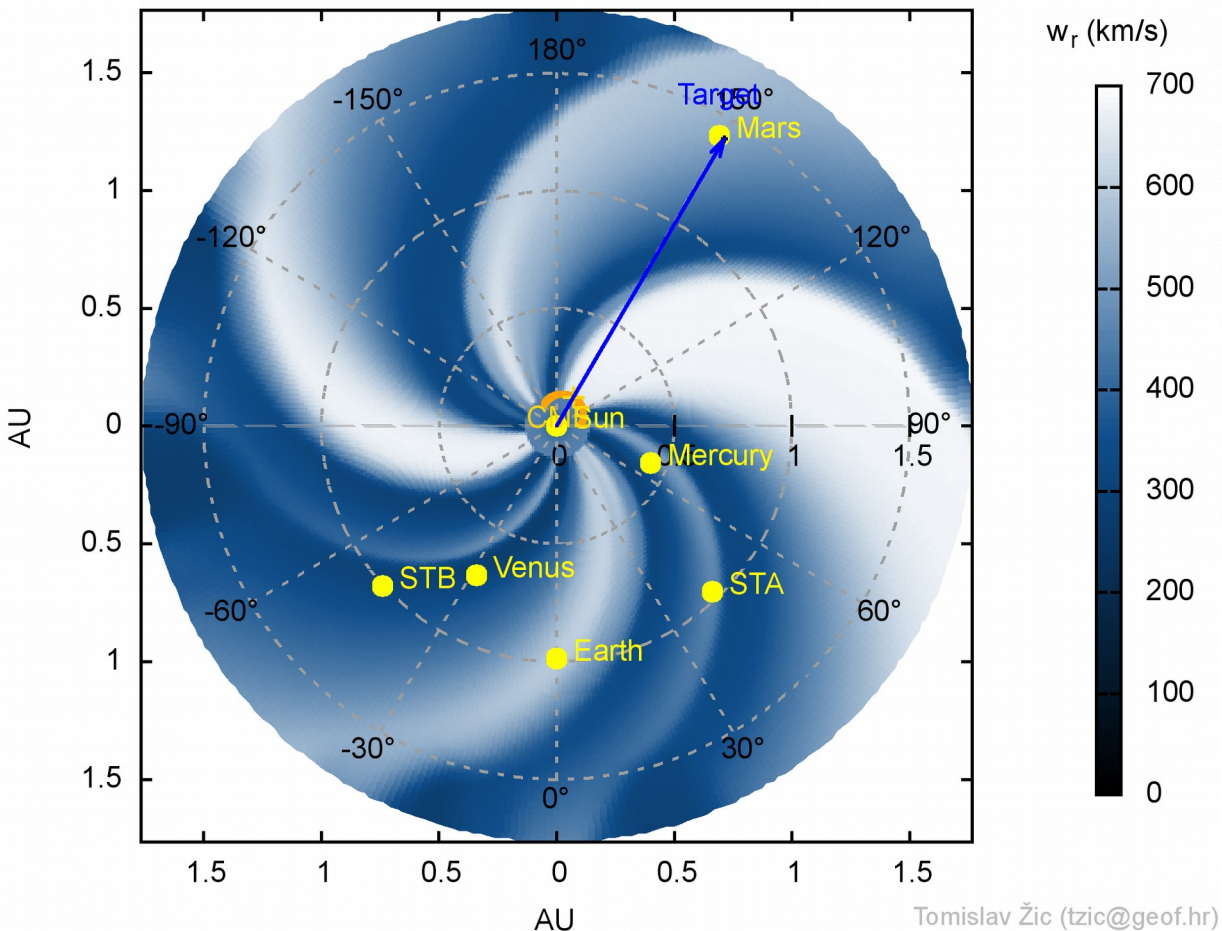
- CME take-off date & time: 12.04.2016 at 16h:00min
- $\gamma_\infty = 0.2 \times 10^{-7} \text{ km}^{-1}$, $w_\infty = 450 \text{ km/s}$,
- $R_0 = 20 r_S$, $v_0 = 1000 \text{ km/s}$,
 $\lambda = 30^\circ$, $\varphi_{\text{CME}} = 0^\circ$
- $R_{\text{target}} = 1 \text{ AU}$, $\varphi_{\text{target}} = 0^\circ$

Calculated in 13.48 seconds.

- LEFT: Cross-section of CME propagation in ecliptic plane
- RIGHT: Propagation of '+ CME' point in geometry plot

Example of DBM + ENLIL model

(<http://oh.geof.unizg.hr/~tomislav/DBM-ENLIL/>)



Tomislav Žic (tzic@geof.hr), Hvar Observatory

$w(R), \gamma(R) \rightarrow$ CME-edge flattening

- drag parameter: $\Gamma = 0.2$
- initial CME distance:
 $R_0 = 31 r_s$
- initial CME speed:
 $v_0 = 1000 \text{ km/s}$
- CME half-width: $\lambda = 60^\circ$
- launching CME meridian distance:
 $\varphi = 150^\circ$
- target: Mars

- LEFT: Cross-section of CME propagation in ecliptic plane. The CME take-off time: February the 10th, 2009 at 06:13 UT.
- RIGHT: Propagation of '+ CME' point in geometry plot

Automatic Fitting

- INPUT: observed ICME dataset: $\{(R_0, v_0), \dots, (R_N, v_N)\}$
- OUTPUT: DBM parameters $(\Gamma, w_\infty, R_0, v_0)$
- The least-square fitting (LSF):
 - successive variation of DBM parameters \rightarrow minimal deviation between observed v_i and DBM-calculated speeds $v(R_i)$:

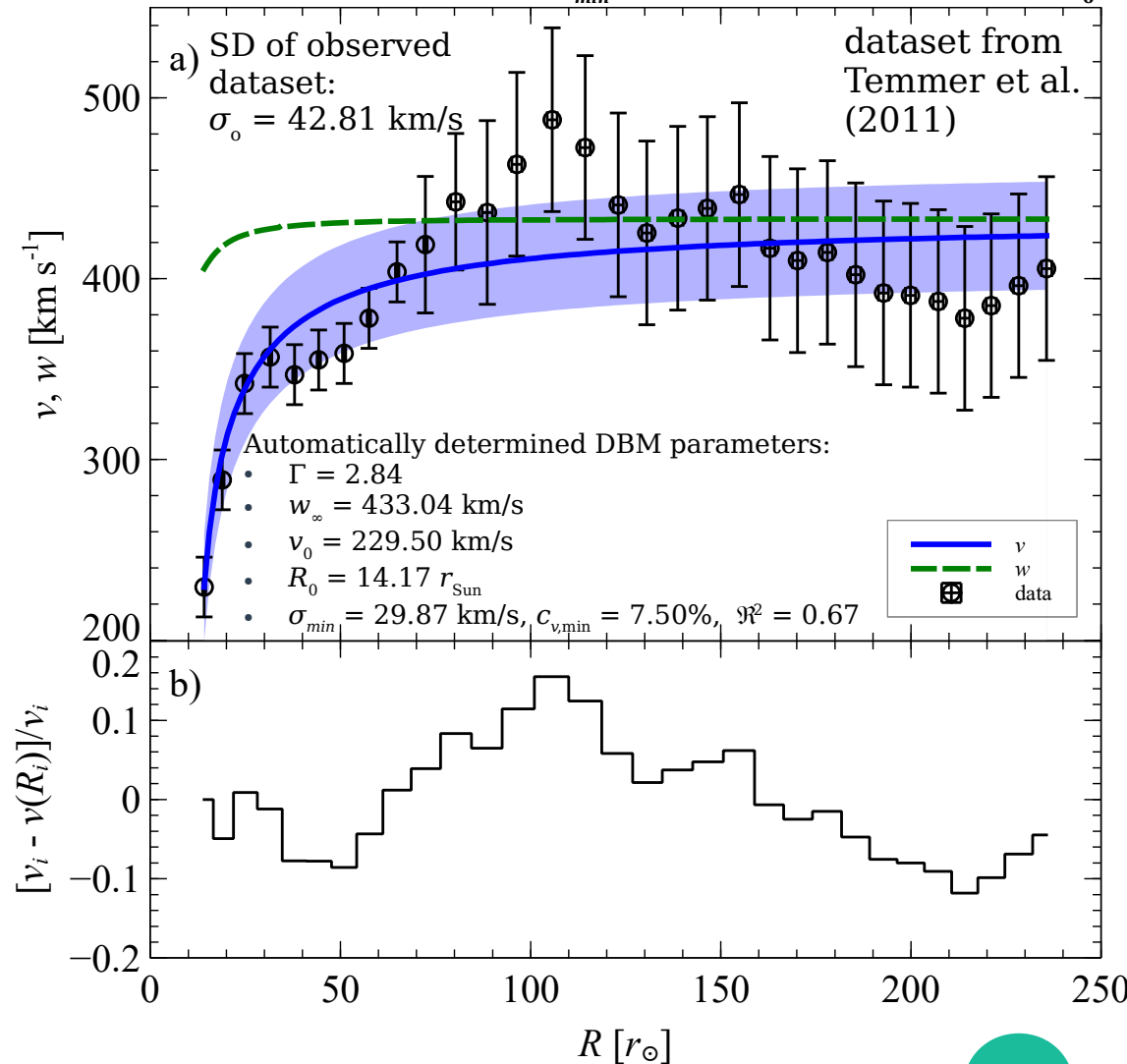
$$\sigma(\Gamma, w_\infty, R_0, v_0) = \sqrt{\frac{1}{(N+1)} \sum_{i=0}^N [v_i - v(R_i)]^2}$$

$\rightarrow \sigma_{\min} \rightarrow$

\rightarrow the best $(\Gamma, w_\infty, R_0, v_0)$

- for real-time space-weather forecasting (successive fitting as ICME propagates)

The fitted standard deviation σ_{\min} is smaller than the observed σ_o !



Conclusion

- The drag-based model is useful because:
 - it is simple, fast and versatile
 - its accuracy is not worse in comparison to the other advanced models (Vršnak et al., 2014)
 - it is suited for a fast real-time space-weather forecasting (Žic et al., 2015)
- Drawbacks:
 - the magnetic field/Lorentz force is not included in the DBM
 - CME-CME interaction is problematic for calculation
 - the DBM is not basically designed for usage in a complex heliospheric environment
(Will DBM + ENLIL provide better forecasting results?)

**Thank you
for your
attention!**

References

- Borgazzi, A., Lara, A., Echer, E., Alves, M.V.: 2009, *Dynamics of coronal mass ejections in the interplanetary medium*. *Astron. Astrophys.* 498, 885 – 889.
- Cargill, P.J.: 2004, *On the Aerodynamic Drag Force Acting on Interplanetary Coronal Mass Ejections*. *Solar Phys.* 221, 135 – 149.
- Davies, J.A., Harrison, R.A., Perry, C.H., Möstl, C., Lugaz, N., Rollett, T., Davis, C.J., Crothers, S.R., Temmer, M., Eyles, C.J., Savani, N.P.: 2012, *A Self-similar Expansion Model for Use in Solar Wind Transient Propagation Studies*. *Astrophys. J.* 750, 23.
- Gopalswamy, N., Lara, A., Lepping, R.P., Kaiser, M.L., Berdichevsky, D., Cyr, O.C.S.: 2000, *Interplanetary acceleration of coronal mass ejections*. *Geophys. Res. Lett.* 27, 145 – 148.
- Lara, A., Borgazzi, A.I.: 2009, *Dynamics of interplanetary CMEs and associated type II bursts*. In: N. Gopalswamy & D. F. Webb (ed.) *IAU Symposium, IAU Symposium 257*, 287 – 290.
- Leblanc, Y., Dulk, G.A., Bougeret, J.-L.: 1998, *Tracing the Electron Density from the Corona to 1 au*. *Solar Phys.* 183, 165 – 180.
- Lugaz, N., Hernandez-Charpak, J.N., Roussev, I.I., Davis, C.J., Vourlidas, A., Davies, J.A.: 2010, *Determining the Azimuthal Properties of Coronal Mass Ejections from Multi-Spacecraft Remote-Sensing Observations with STEREO SECCHI*. *Astrophys. J.* 715, 493 – 499.
- Möstl, C., Davies, J.A.: 2012, *Speeds and Arrival Times of Solar Transients Approximated by Self-similar Expanding Circular Fronts*. *Solar Phys.*, 77.
- Owens, M., Cargill, P.: 2004, *Predictions of the arrival time of Coronal Mass Ejections at 1AU: an analysis of the causes of errors*. *Annales Geophysicae* 22, 661 – 671.
- Schwenn, R., dal Lago, A., Huttunen, E., Gonzalez, W.D.: 2005, *The association of coronal mass ejections with their effects near the Earth*. *Ann. Geophys.* 23, 1033 – 1059.
- Thernisien, A.: 2011, *Implementation of the Graduated Cylindrical Shell Model for the Three-dimensional Reconstruction of Coronal Mass Ejections*. *Astrophys. J. Supp.* 194, 33.
- Thernisien, A.F.R., Howard, R.A., Vourlidas, A.: 2006, *Modeling of Flux Rope Coronal Mass Ejections*. *Astrophys. J.* 652, 763 – 773.
- Vršnak, B.: 2001, *Deceleration of Coronal Mass Ejections*. *Solar Phys.* 202, 173 – 189.
- Vršnak, B., Žic, T.: 2007, *Transit times of interplanetary coronal mass ejections and the solar wind speed*. *Astron. Astrophys.* 472, 937 – 943.
- Vršnak, B., Žic, T., Falkenberg, T.V., Möstl, C., Vennerstrom, S., Vrbanec, D.: 2010, *The role of aerodynamic drag in propagation of interplanetary coronal mass ejections*. *Astron. Astrophys.* 512, A43.
- Vršnak, B., Žic, T., Vrbanec, D., Temmer, M., Rollett, T., Möstl, C., Veronig, A., Čalogović, J., Dumbović, M., Lulić, S., Moon, Y.-J., Shanmugaraju, A.: 2013, *Propagation of Interplanetary Coronal Mass Ejections: The Drag-Based Model*. *Solar Phys.* 285, 295 – 315.
- Žic, T., Vršnak, B., Temmer, M.: 2015, *Heliospheric Propagation of Coronal Mass Ejections: Drag-based Model Fitting*. *Astrophys. J. Supp.* 218, 32.